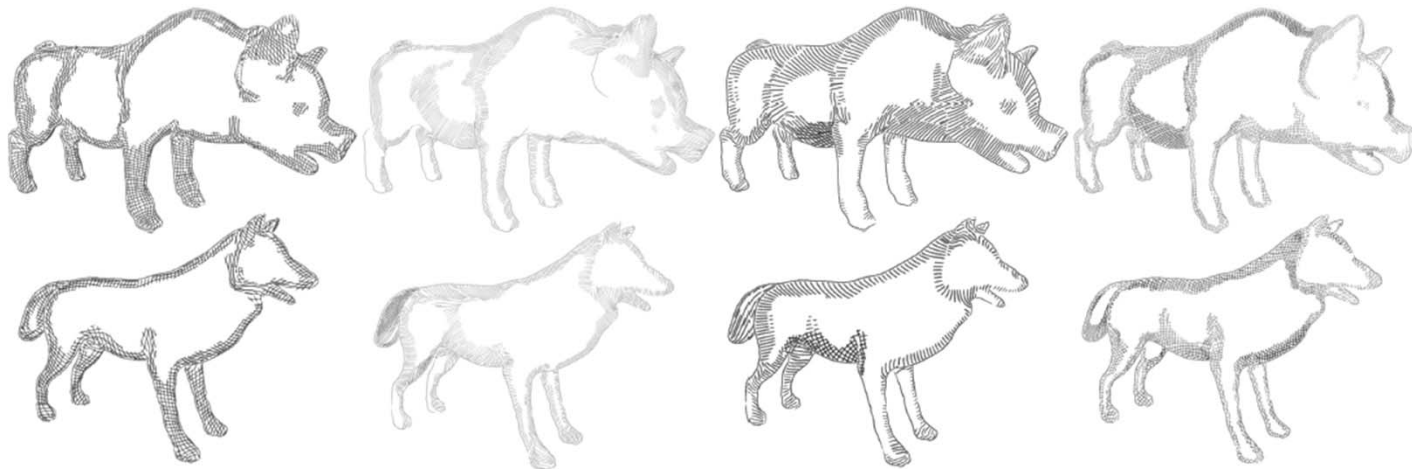


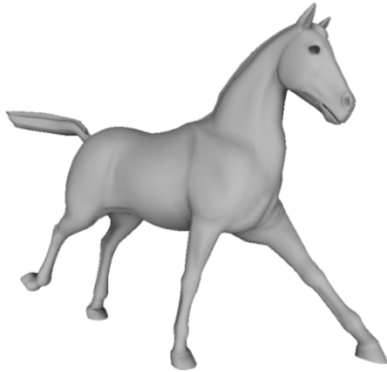
Learning hatching for pen-and-ink illustrations of surfaces



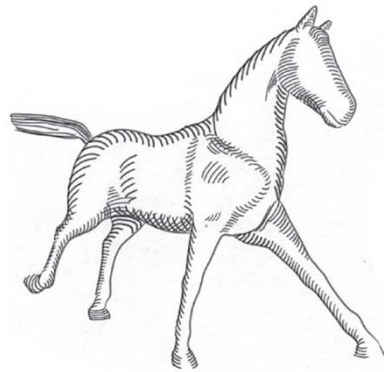
Evangelos Kalogerakis^{1,2}, Derek Nowrouzehahrai^{1,3,4},
Simon Breslav^{1,5}, Aaron Hertzmann¹

¹University of Toronto, ²Stanford University, ³Disney Research Zurich,
⁴University of Montreal, ⁵Autodesk Research

Goal: Synthesis of hatching illustrations

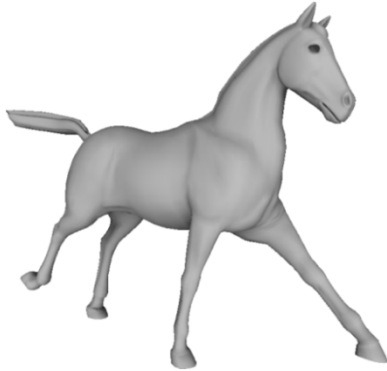


Exemplar shape

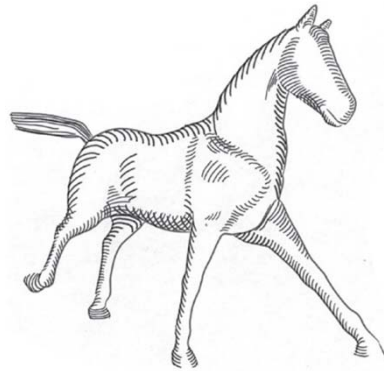


Artist's illustration

Goal: Synthesis of hatching illustrations



Exemplar shape

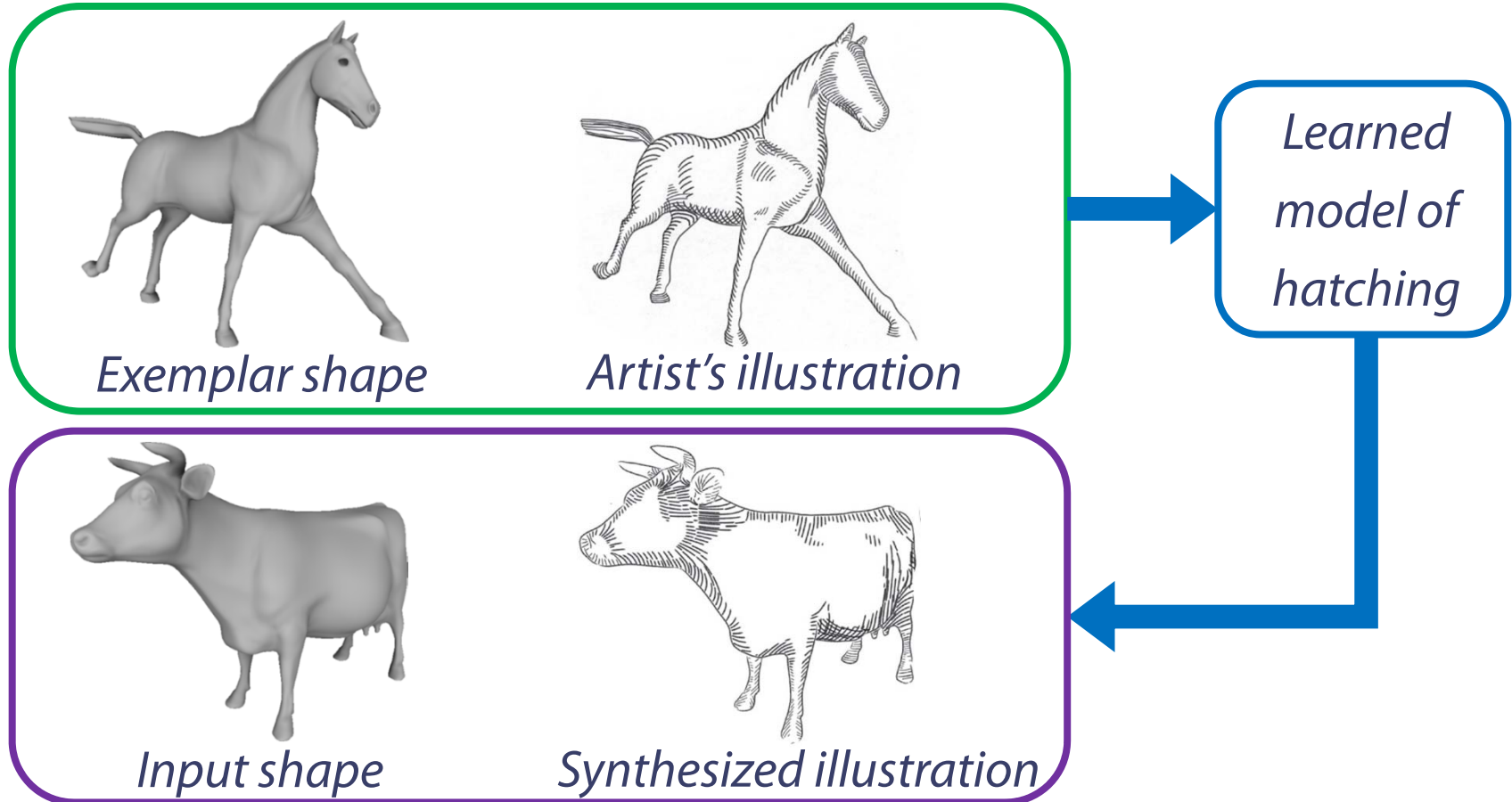


Artist's illustration

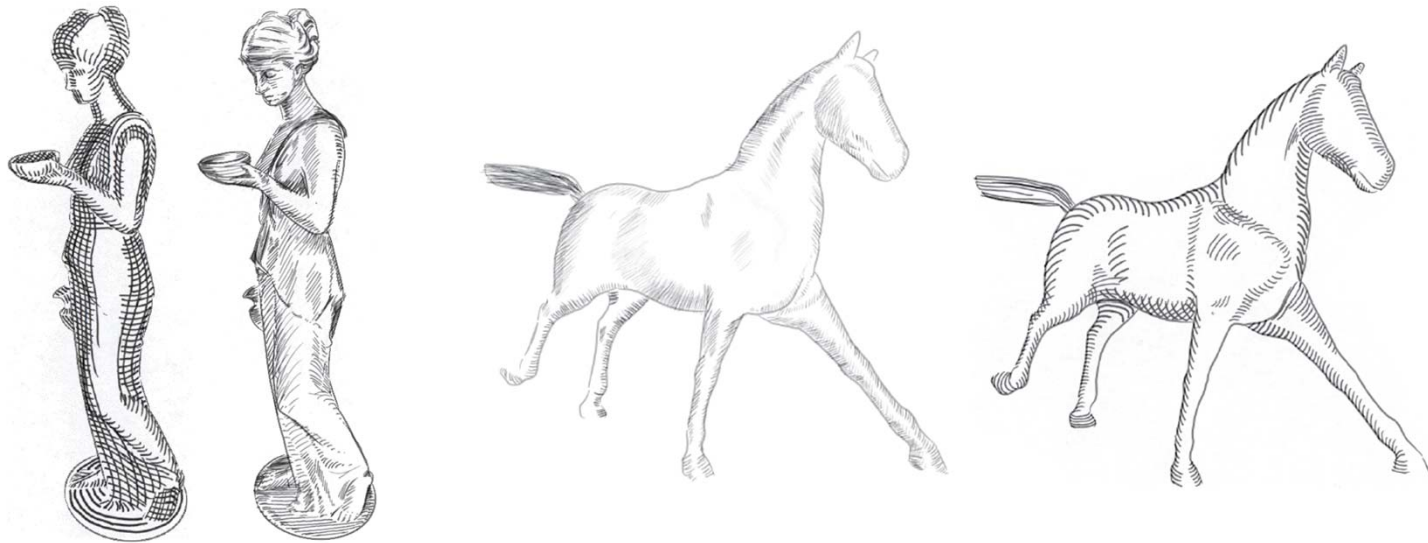


*Learned
model of
hatching*

Goal: Synthesis of hatching illustrations



Challenge: understanding hatching styles



Related work: hatching smooth surfaces



Iso-parametric curves

[Saito and Takahashi 1990, Winkenbach and Salesin 1996]

Related work: hatching smooth surfaces



Iso-parametric curves

[Saito and Takahashi 1990, Winkenbach and Salesin 1996]



Smooth curvature directions and shading-based tone

[Elber 1998, Hertzmann and Zorin 2000]

Related work: hatching smooth surfaces



Iso-parametric curves

[Saito and Takahashi 1990, Winkenbach and Salesin 1996]



Smooth curvature directions and shading-based tone

[Elber 1998, Hertzmann and Zorin 2000]



Shading gradients

[Singh and Schaefer 2010]

Related work: hatching smooth surfaces



Iso-parametric curves

[Saito and Takahashi 1990, Winkenbach and Salesin 1996]



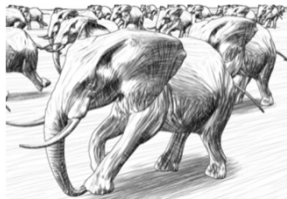
Smooth curvature directions and shading-based tone

[Elber 1998, Hertzmann and Zorin 2000]



Shading gradients

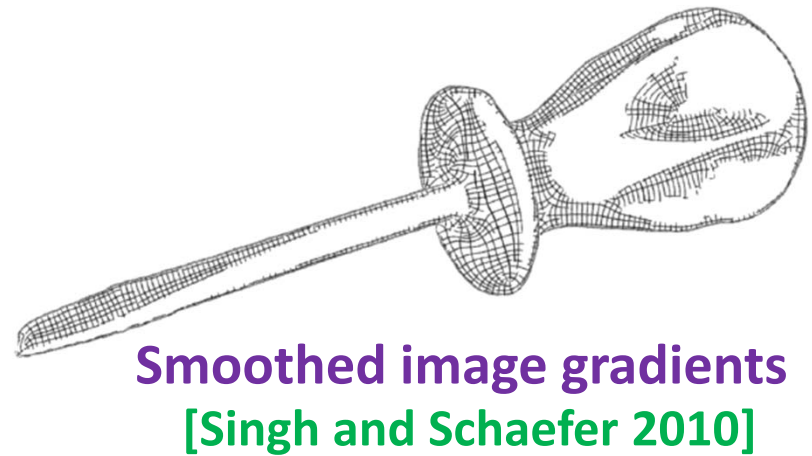
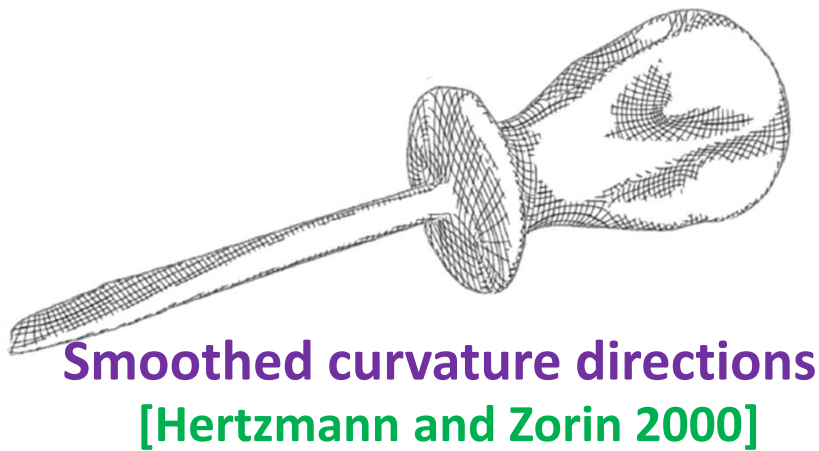
[Singh and Schaefer 2010]



Real-time hatching

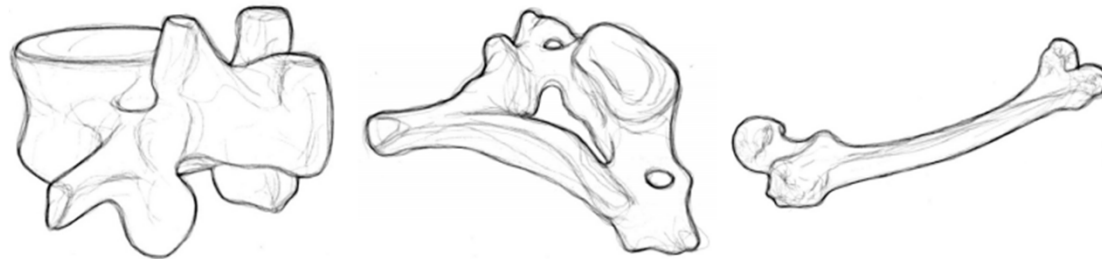
[Praun et al. 2001, Kim et al. 2008]

Related work: hatching smooth surfaces



Related work: where do people draw lines?

[Cole et al. 2008]



Average images composed of artists' drawings



Predicted line drawing

Our approach

Learns a model of hatching style from **a single artist's drawing** of an input shape

Our approach

Learns a model of hatching style from **a single artist's drawing** of an input shape

Can transfer the hatching style to **different views of the exemplar shape** as well as **different shapes**

Our approach

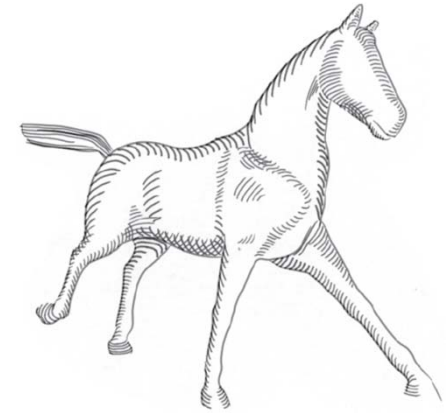
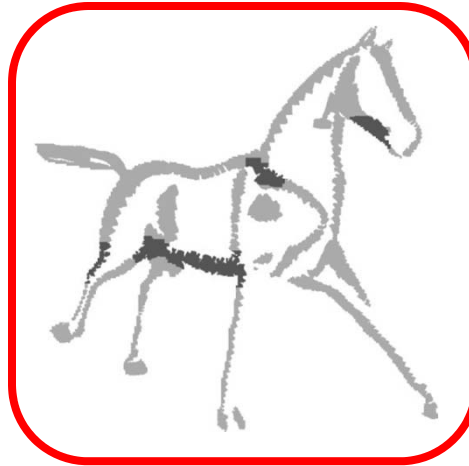
Learns a model of hatching style from **a single artist's drawing** of an input shape

Can transfer the hatching style to **different views of the exemplar shape** as well as **different shapes**

The hatching style is determined by **hatching properties** related to hatching tone and orientations

Hatching properties

Hatching level

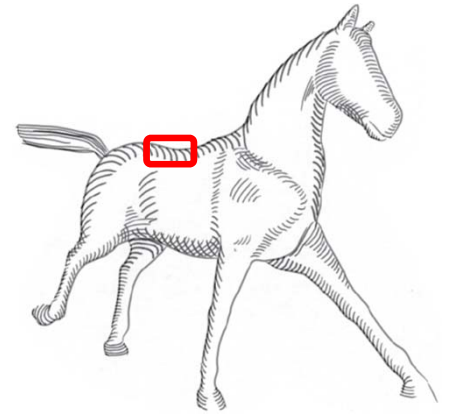
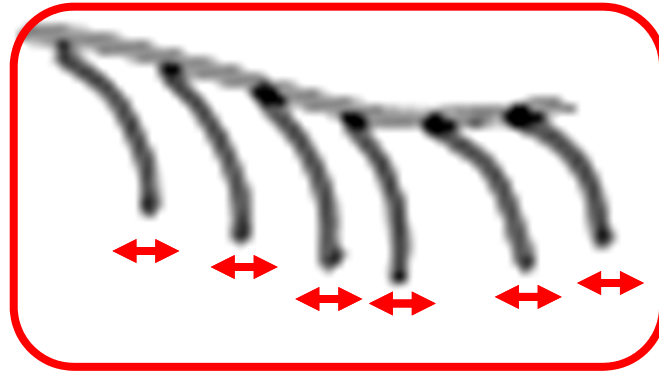


- No hatching
- Hatching
- Cross-hatching

Hatching properties

Hatching level

Stroke thickness

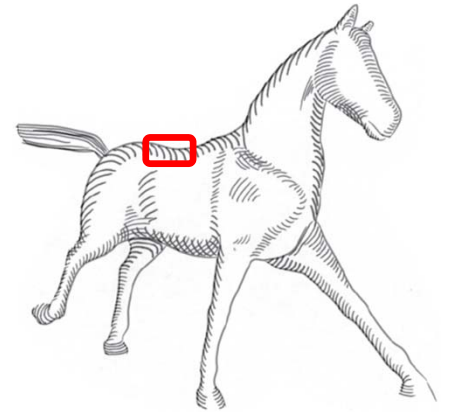
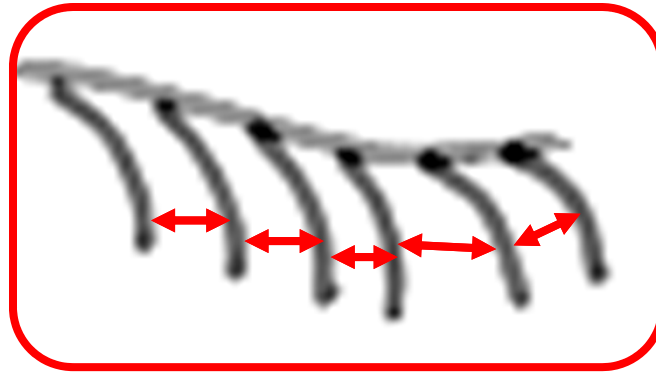


Hatching properties

Hatching level

Stroke thickness

Stroke spacing



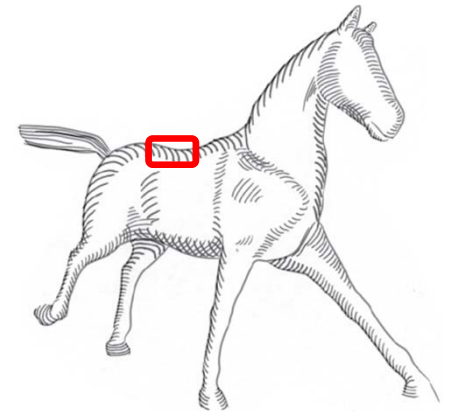
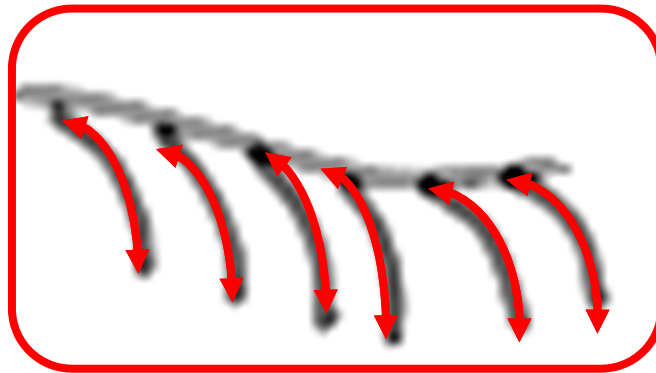
Hatching properties

Hatching level

Stroke thickness

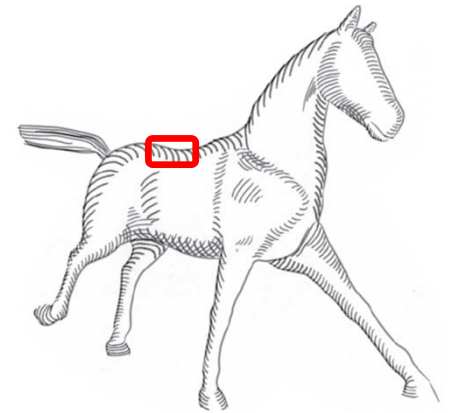
Stroke spacing

Stroke length



Hatching properties

- Hatching level
- Stroke thickness
- Stroke spacing
- Stroke length
- Stroke intensity**



Hatching properties

Hatching level

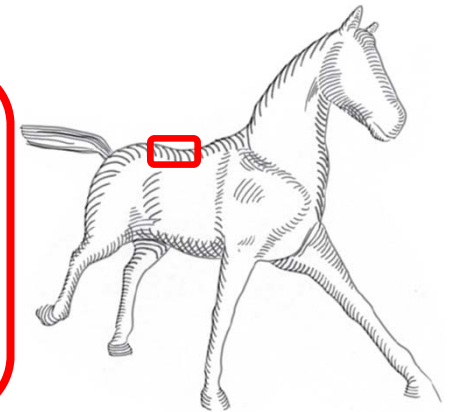
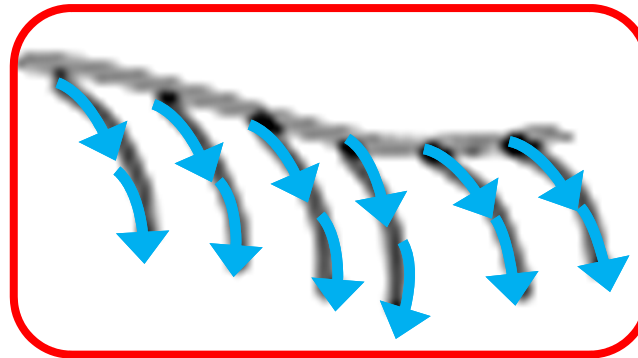
Stroke thickness

Stroke spacing

Stroke length

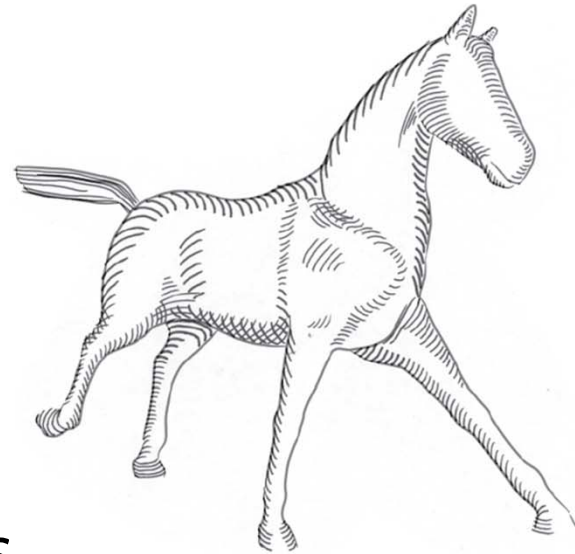
Stroke intensity

Hatching orientations



Hatching properties

Hatching level
Stroke thickness
Stroke spacing
Stroke length
Stroke intensity
Hatching orientations

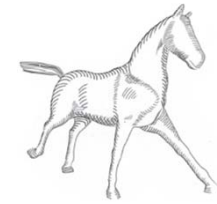


Artist's illustration

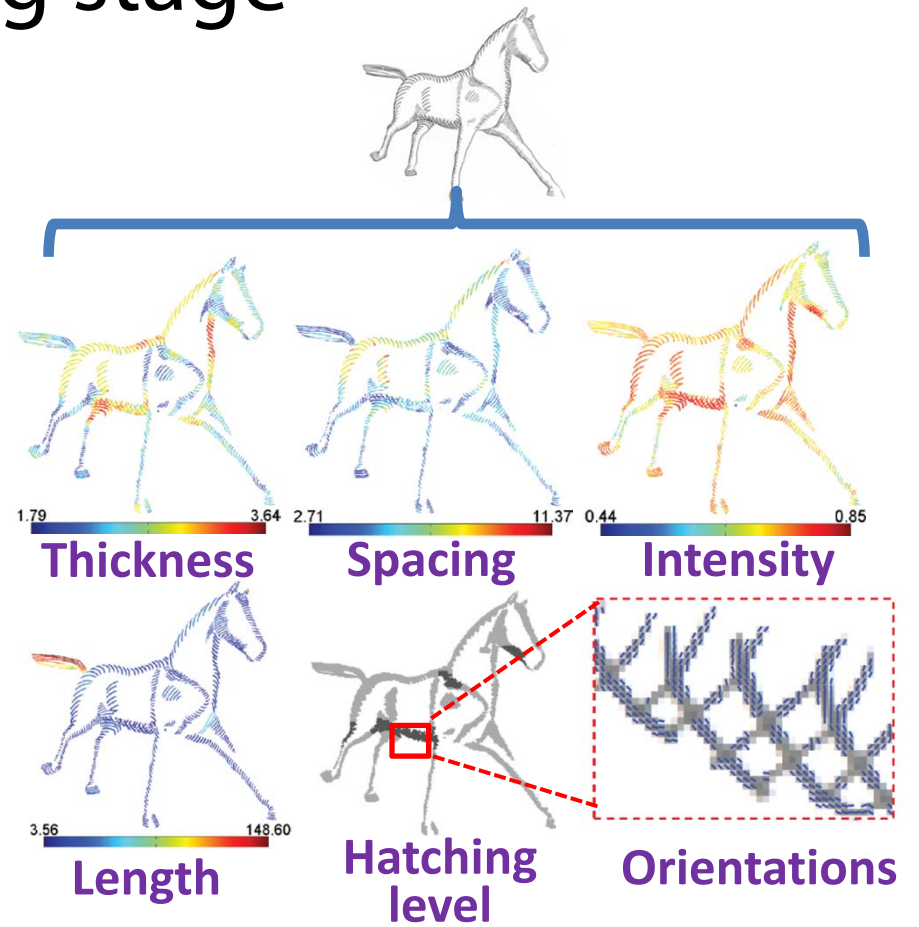


Computer-generated illustration

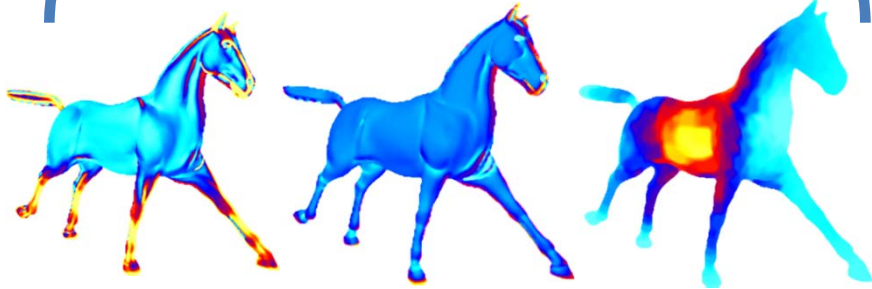
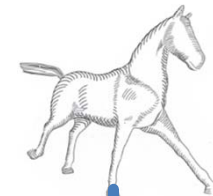
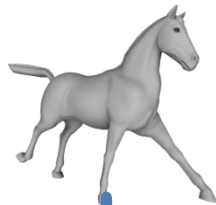
Learning stage



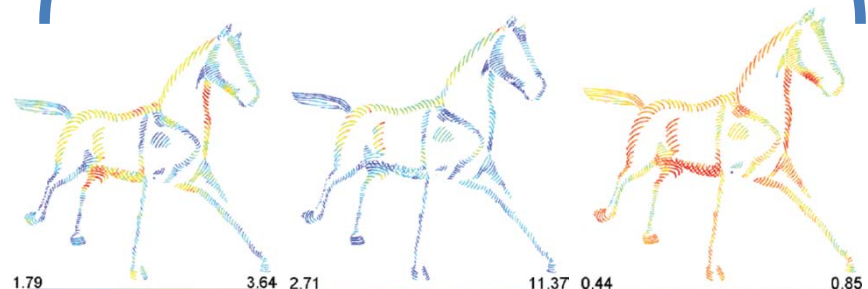
Learning stage



Learning stage



Shape features



Thickness

Spacing

Intensity

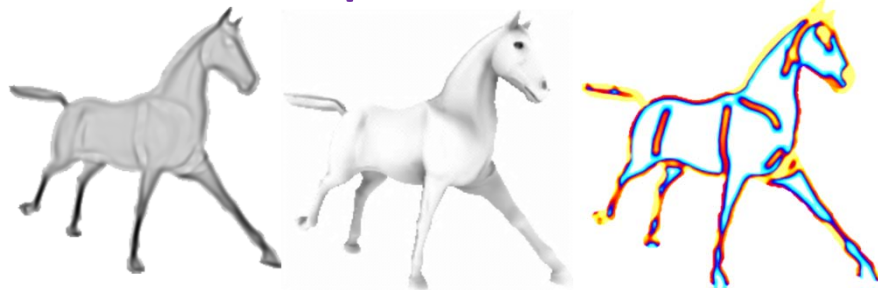
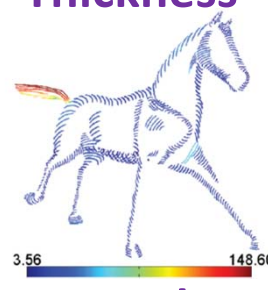
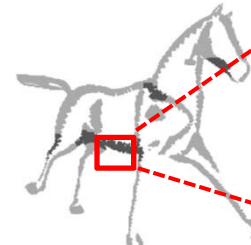


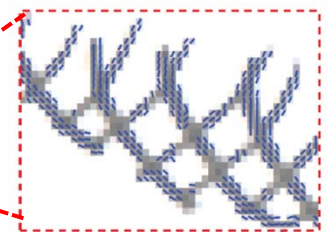
Image-space features



Length



Hatching level



Orientations

Learning stage

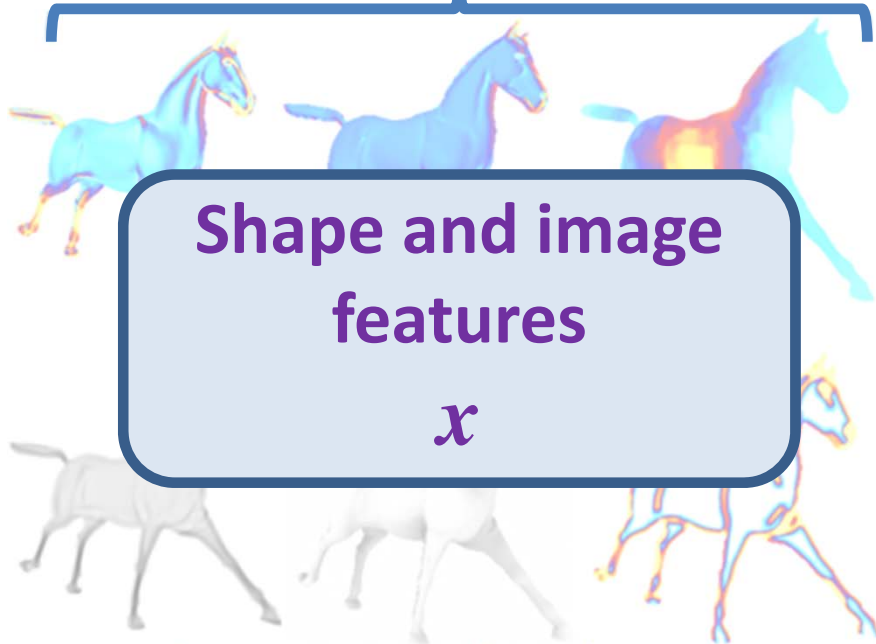
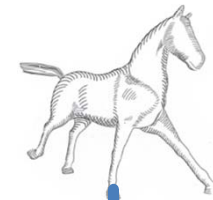
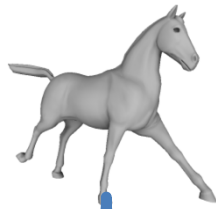


Image-space descriptors

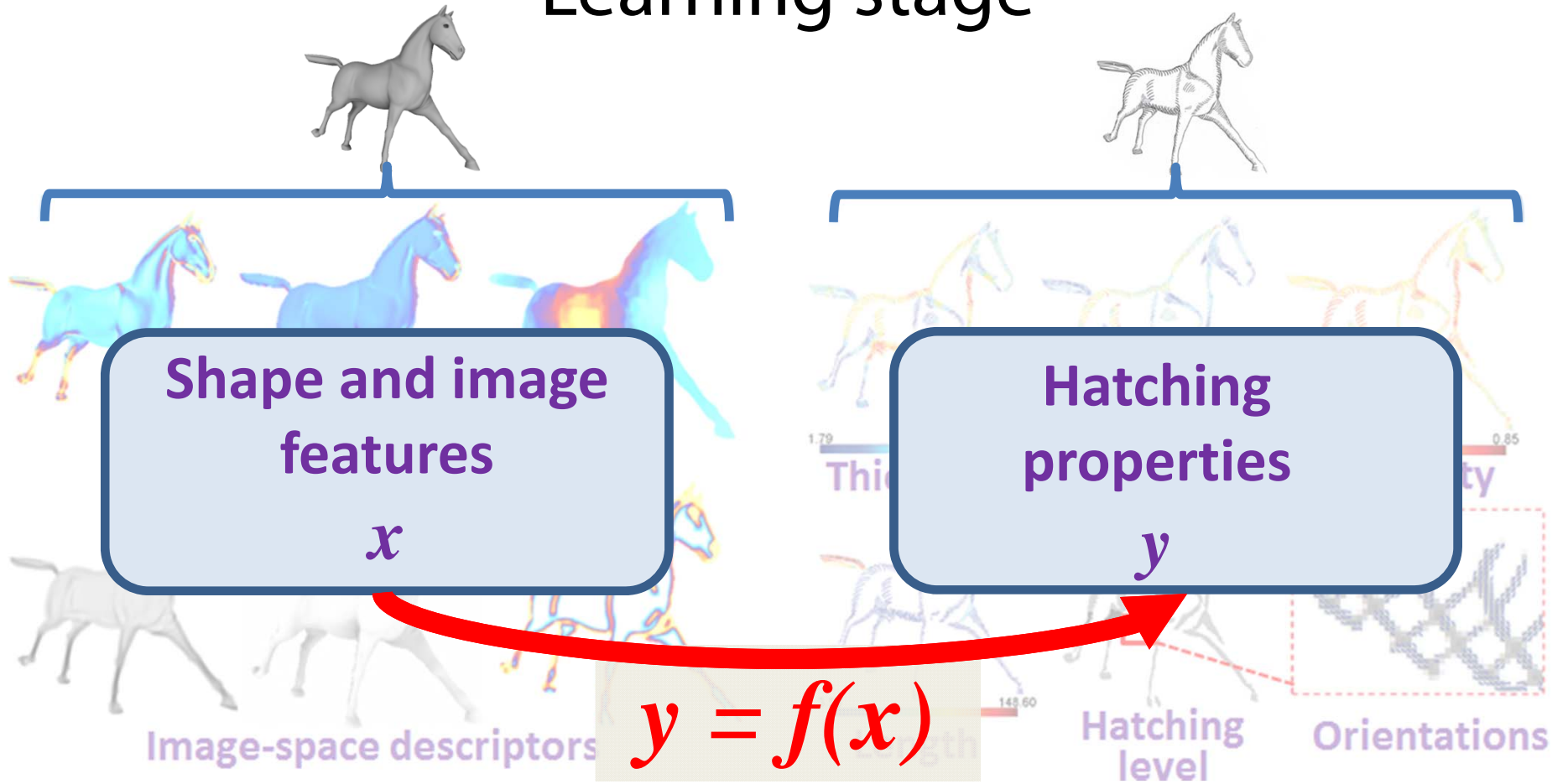
1.79
0.85
3.56 143.60

Length

Hatching level

Orientations

Learning stage



Learning hatching orientations

Linear model expressing hatching orientations as a weighted sum of selected **orientation features**.

$$f(\theta; \mathbf{w}) = \sum_k w_k \mathbf{v}_k$$

$$\mathbf{v} = [\cos(2\theta), \sin(2\theta)]^T$$

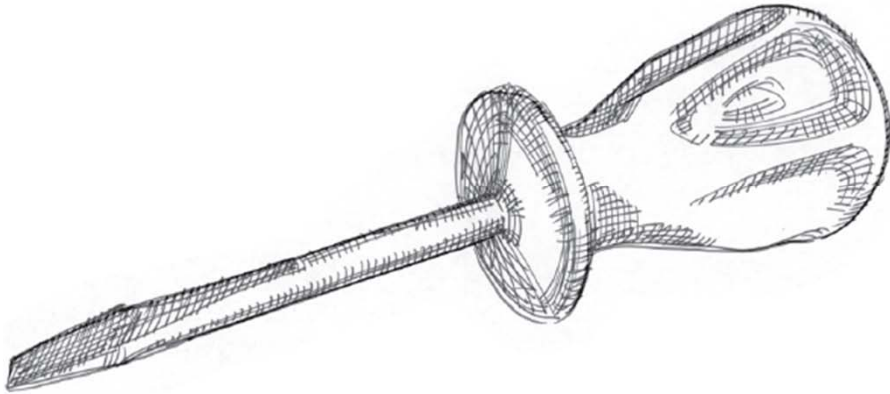
Learning hatching orientations

Linear model expressing hatching orientations as a weighted sum of selected **orientation features**.

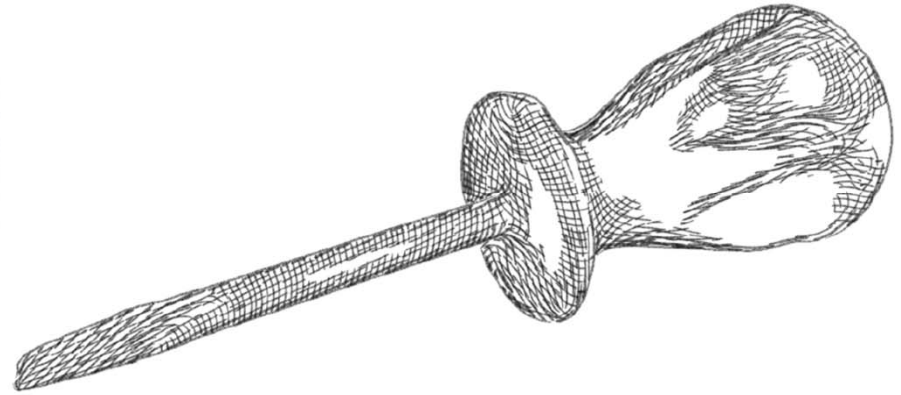
$$f(\theta; \mathbf{w}) = \sum_k w_k \mathbf{v}_k$$

$$\mathbf{v} = [\cos(2\theta), \sin(2\theta)]^T$$

Learning hatching orientations

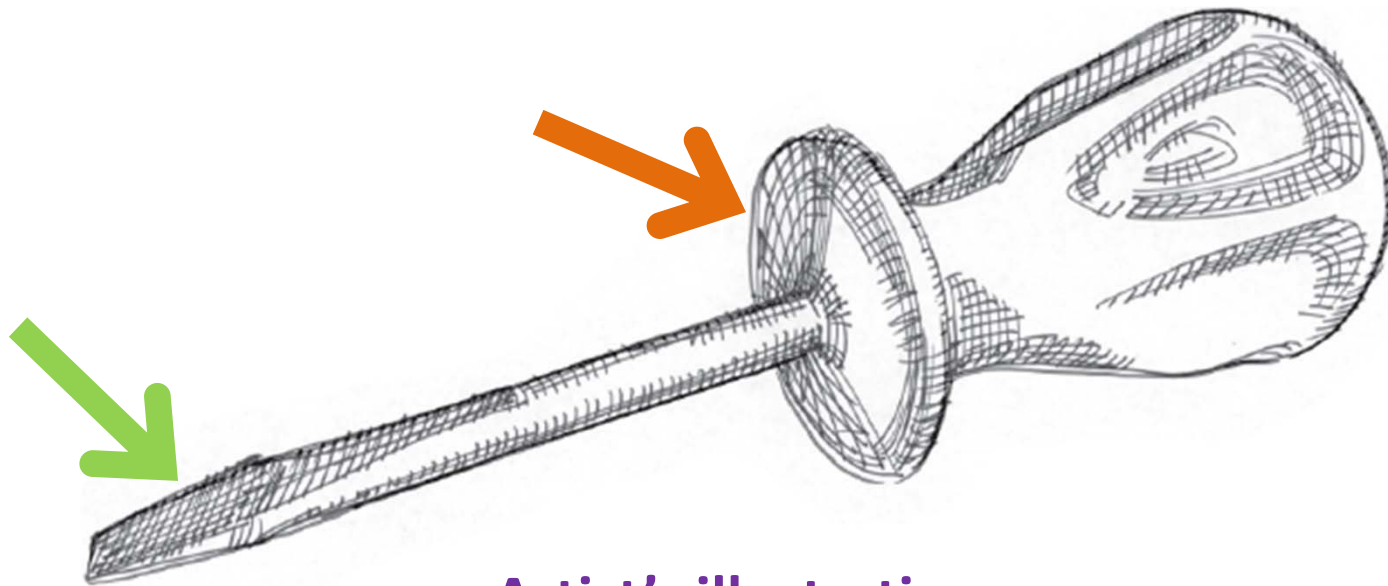


Artist's illustration



**Fitting a single model
across the illustration**

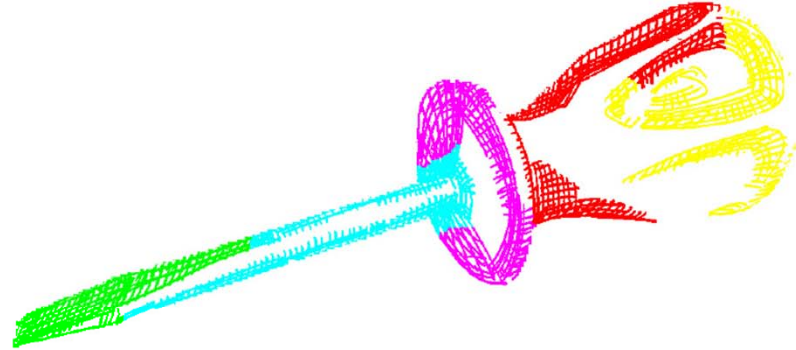
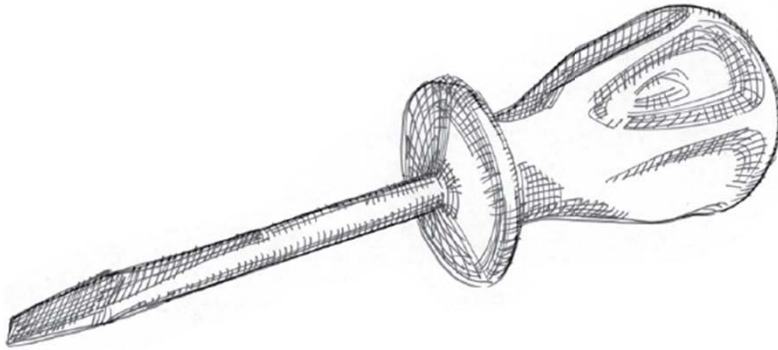
Learning orientation fields



Artist's illustration

Mixture of experts model

Simultaneous segmentation & model fitting for each segment



<div style="display: inline-block; width: 15px; height: 15px; background-color: red; margin-right: 5px;"></div> $\vec{f}_1 = \nabla a_2$ $\vec{f}_2 = .54(\vec{k}_{max,1}) + .46(\vec{r}_\perp)$	<div style="display: inline-block; width: 15px; height: 15px; background-color: cyan; margin-right: 5px;"></div> $\vec{f}_1 = .73(\nabla I_3) + .27(\vec{r})$ $\vec{f}_2 = .69(\vec{k}_{max,2}) + .31(\nabla I_{\perp,3})$	<div style="display: inline-block; width: 15px; height: 15px; background-color: green; margin-right: 5px;"></div> $\vec{f}_1 = .77(\vec{e}_{b,3}) + .23(\nabla I_3)$ $\vec{f}_2 = \vec{v}$
<div style="display: inline-block; width: 15px; height: 15px; background-color: yellow; margin-right: 5px;"></div> $\vec{f}_1 = .59(\vec{e}_{b,3}) + .41(\nabla(\vec{L} \cdot \vec{N})_3)$ $\vec{f}_2 = .63(\vec{e}_{a,3}) + .37(\nabla(\vec{L} \cdot \vec{N})_{\perp,3})$	<div style="display: inline-block; width: 15px; height: 15px; background-color: purple; margin-right: 5px;"></div> $\vec{f}_1 = .88(\nabla a_3) + .12(\nabla(\vec{L} \cdot \vec{N})_3)$ $\vec{f}_2 = .45(\vec{k}_{max,2}) + .31(\nabla a_{\perp,3}) + .24(\vec{e}_{a,3})$	

Learning stroke properties

Map features to thickness, intensity, spacing, length

$$y = \prod_k (a_k x_k + b_k)^{\alpha_k}$$

Learning stroke properties

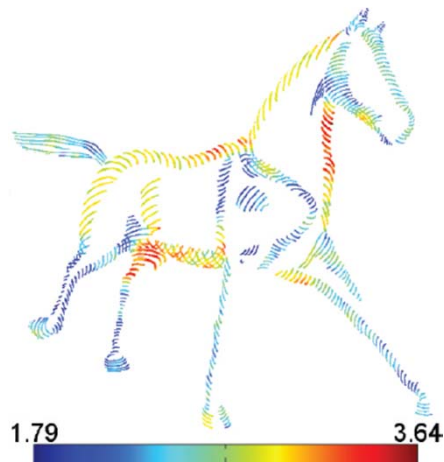
Map features to thickness, intensity, spacing, length

$$y = \prod_k (a_k x_k + b_k)^{\alpha_k}$$

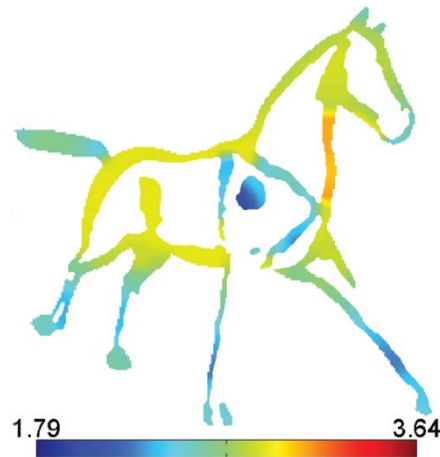
Learning stroke properties

Map features to **thickness**

$$y = \prod_k (a_k x_k + b_k)^{\alpha_k}$$



Extracted thickness

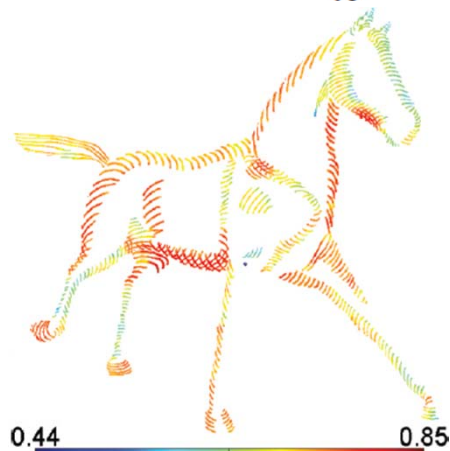


Learned thickness

Learning stroke properties

Map features to **intensity**

$$y = \prod_k (a_k x_k + b_k)^{\alpha_k}$$



Extracted intensity

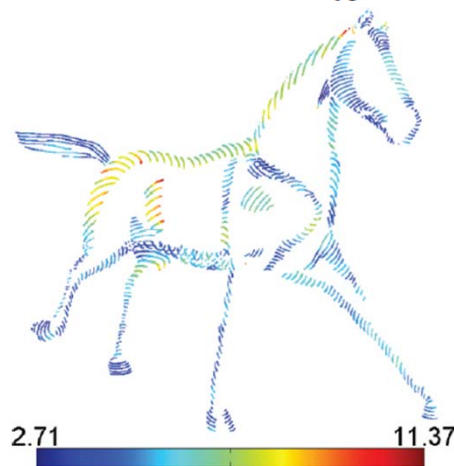


Learned intensity

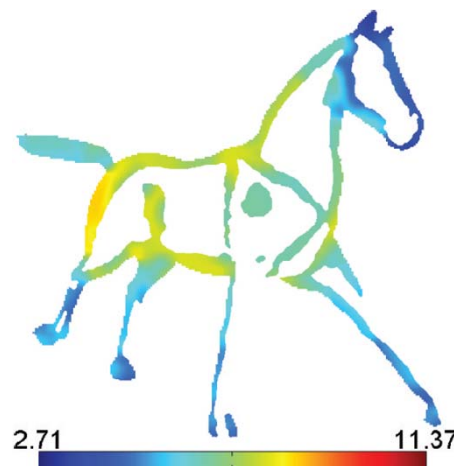
Learning stroke properties

Map features to **spacing**

$$y = \prod_k (a_k x_k + b_k)^{\alpha_k}$$



Extracted spacing

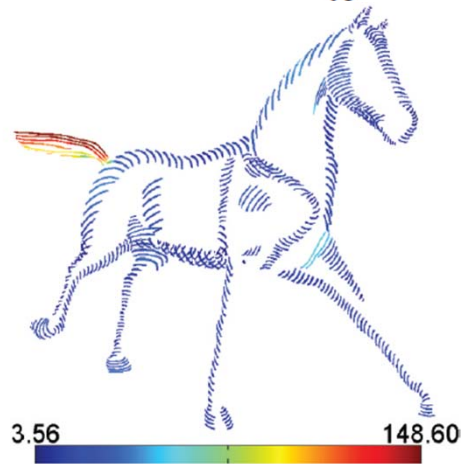


Learned spacing

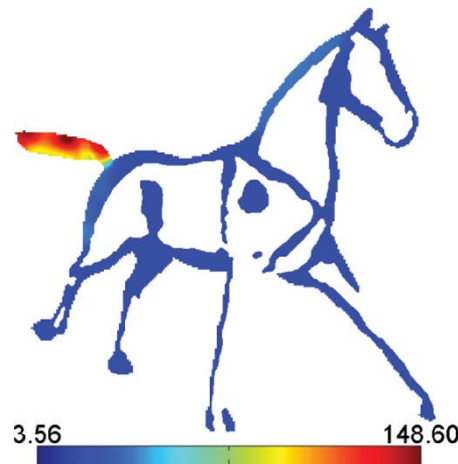
Learning stroke properties

Map features to **length**

$$y = \prod_k (a_k x_k + b_k)^{\alpha_k}$$



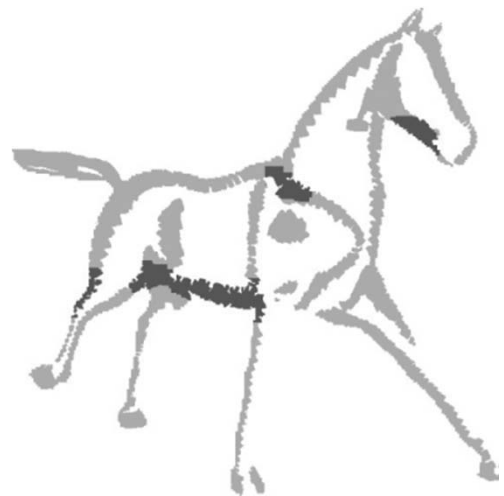
Extracted length



Learned length

Learning hatching level and segment labels

Map features to discrete values with Joint Boosting + CRF



Extracted hatching level



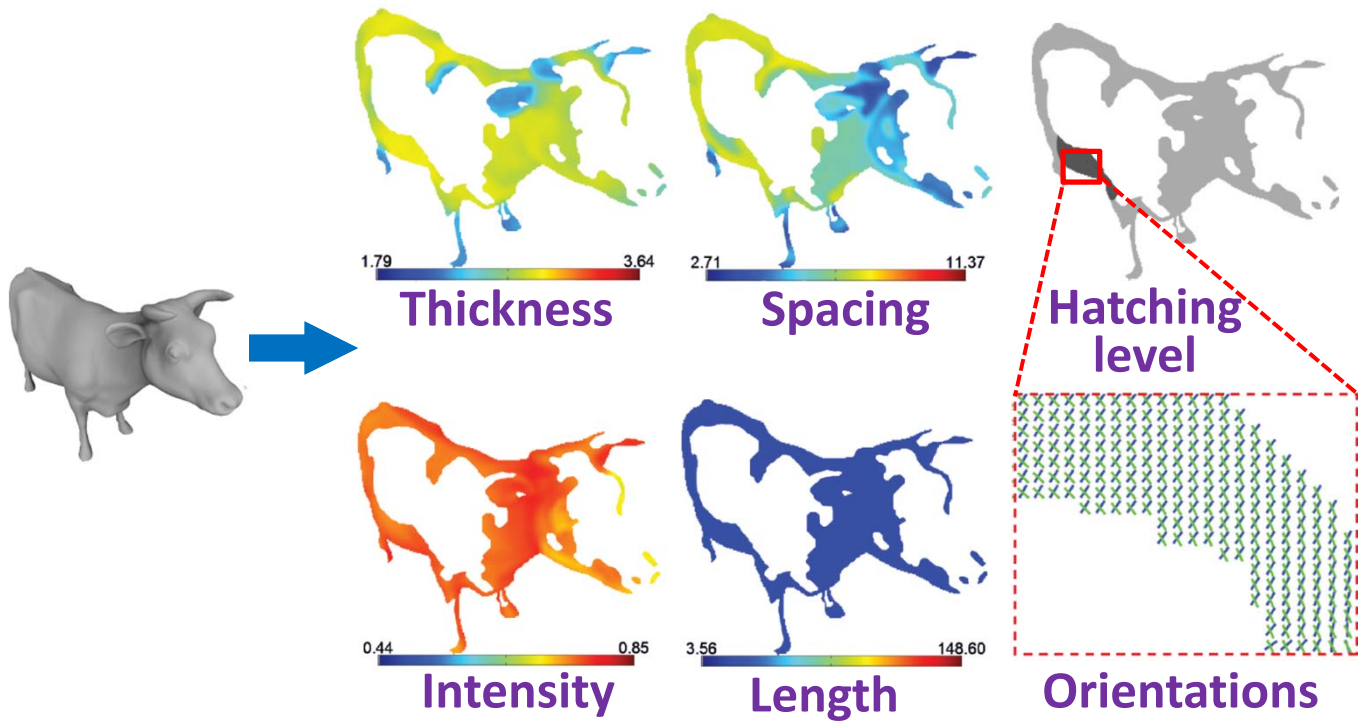
Learned hatching level



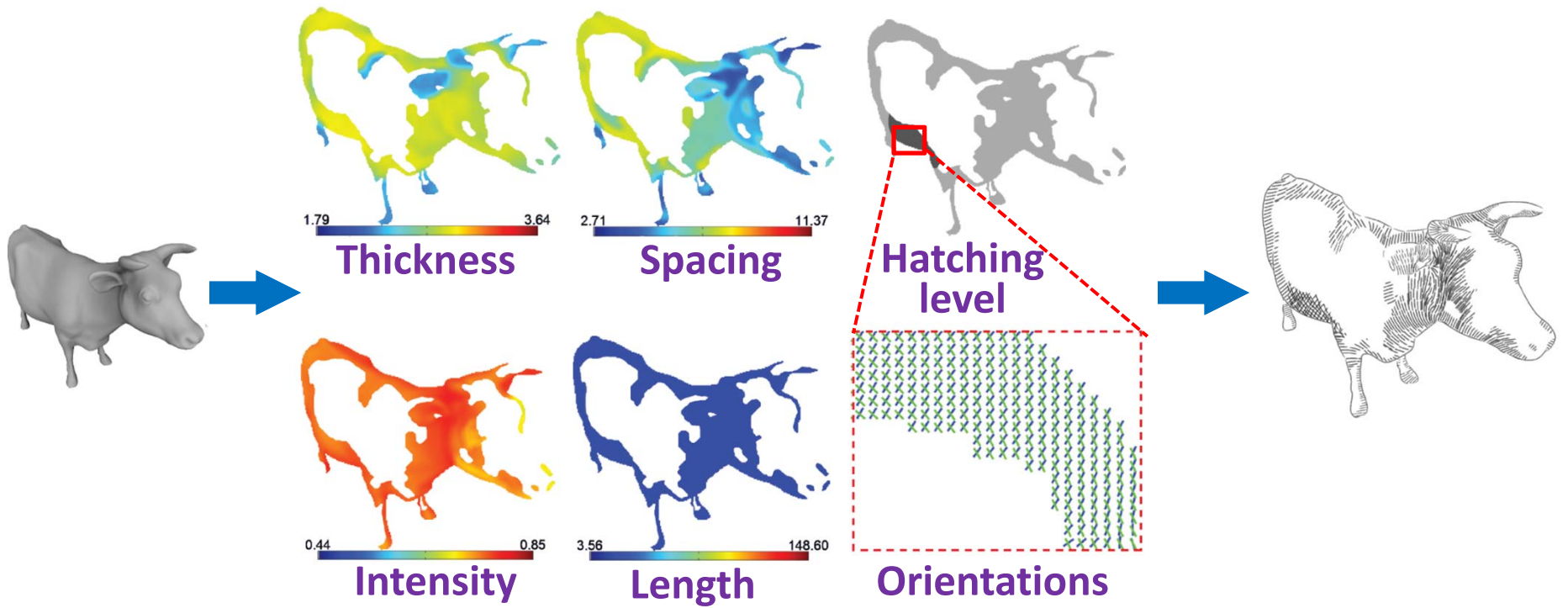
Synthesis stage

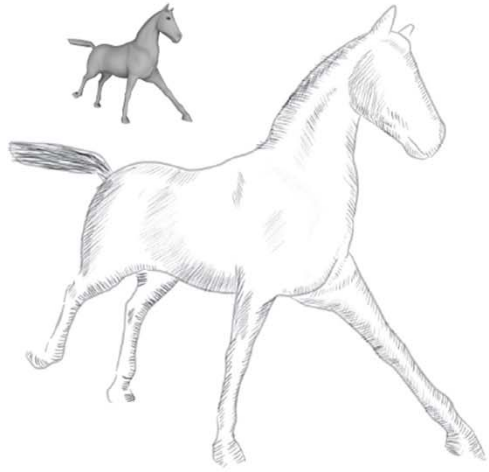


Synthesis stage

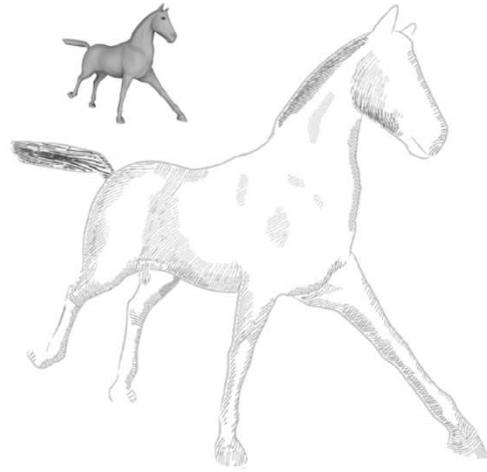
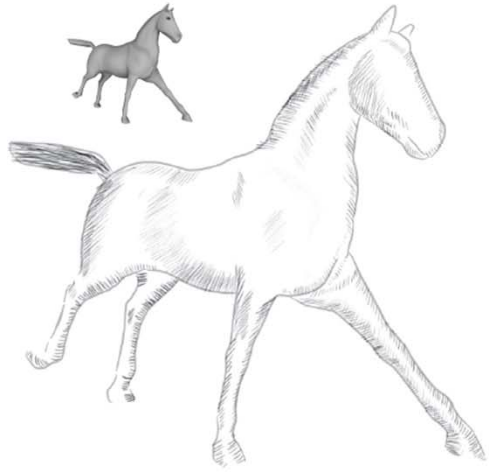


Synthesis stage

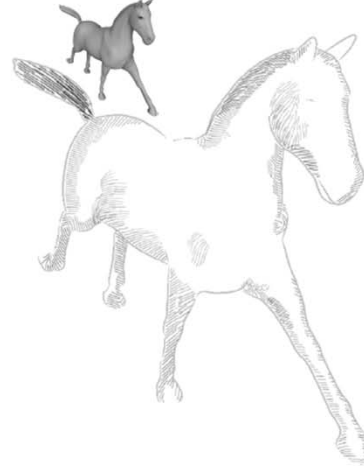
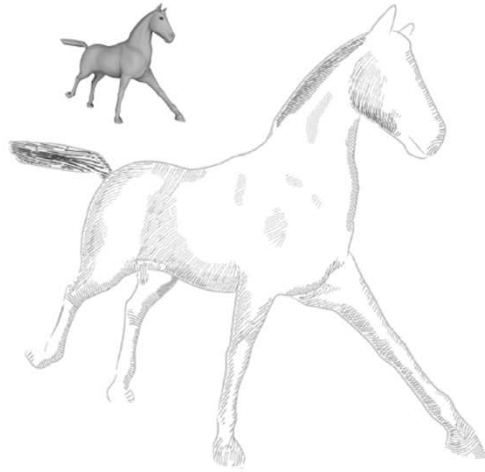
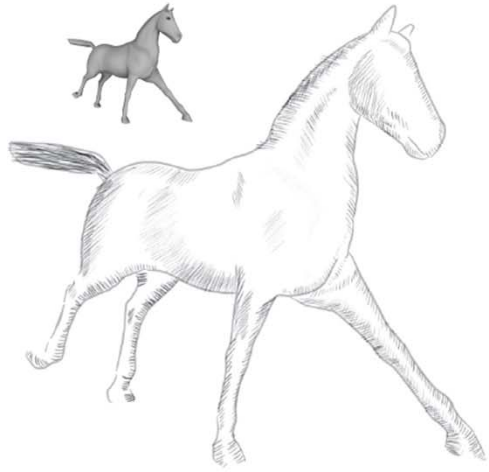




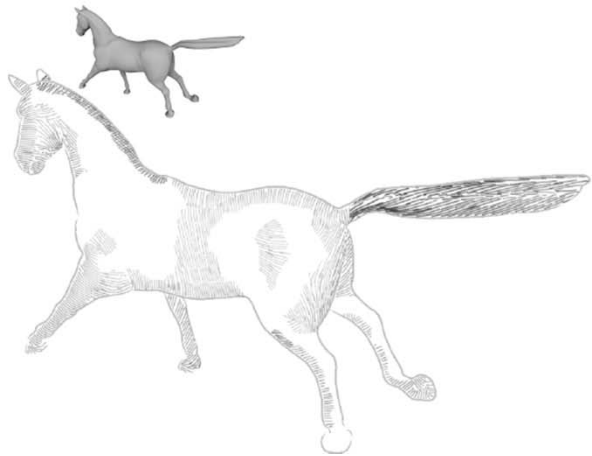
Artist's illustration

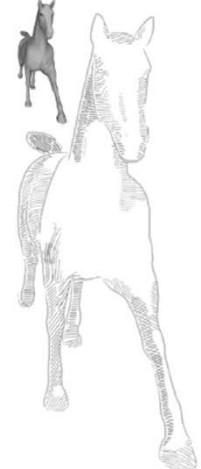
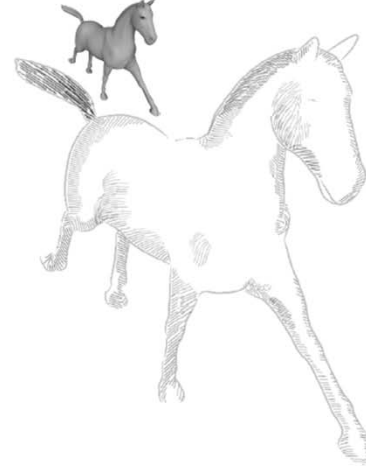
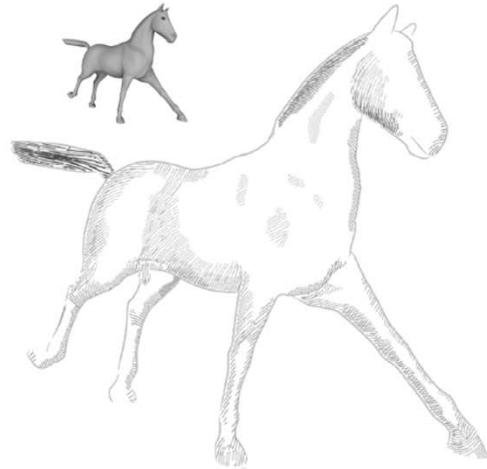
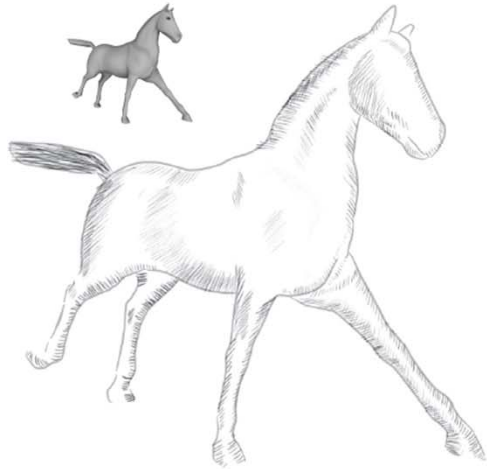


Artist's illustration

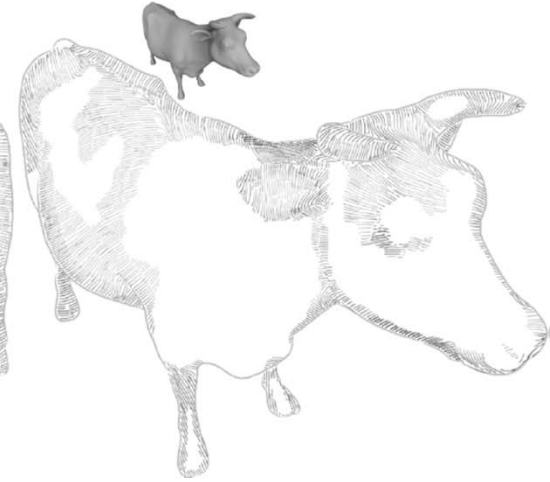
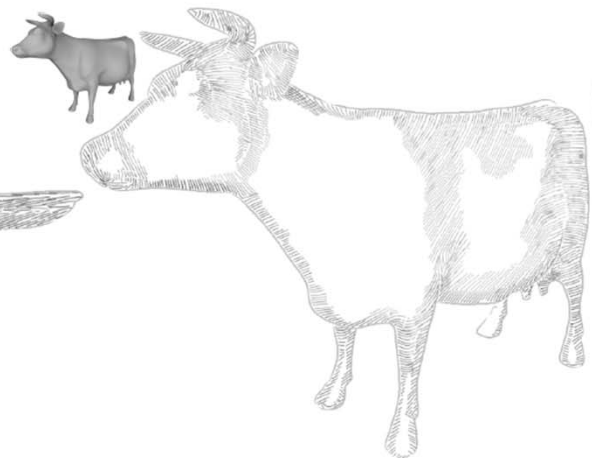
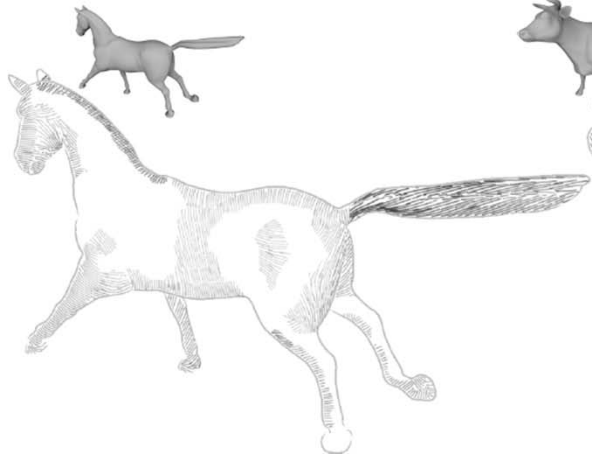


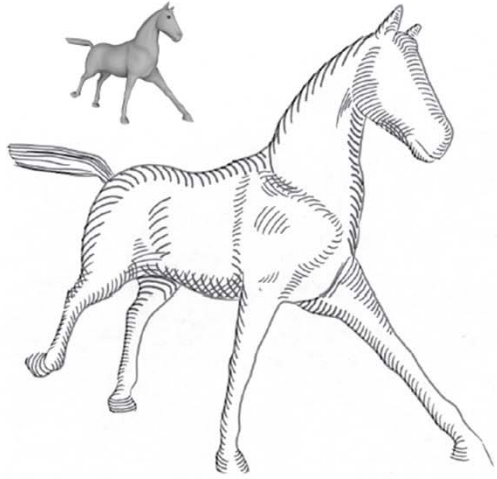
Artist's illustration



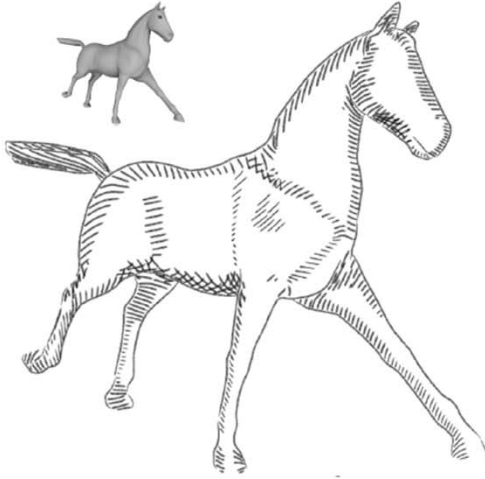
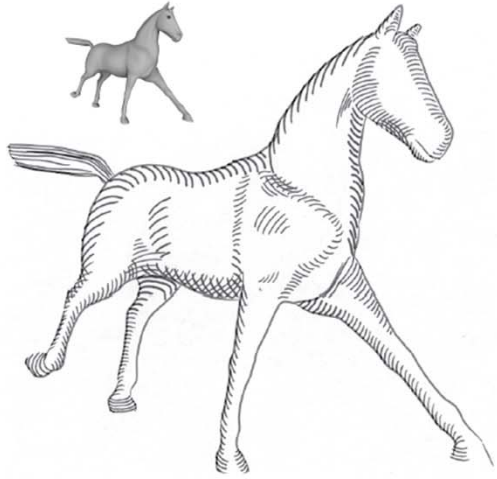


Artist's illustration

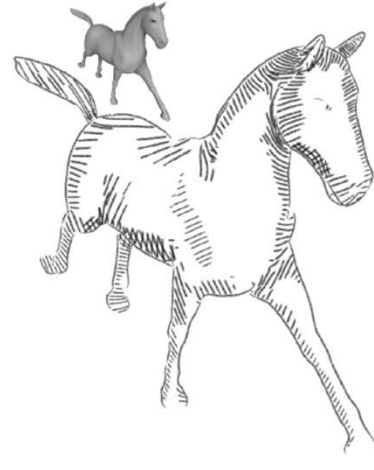
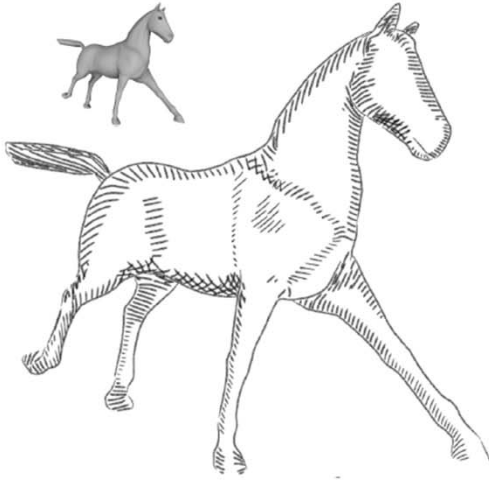
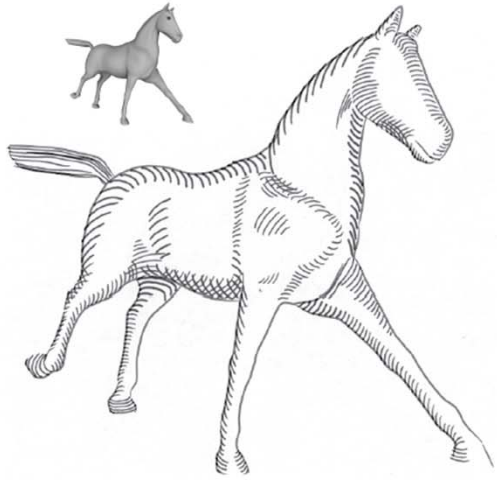




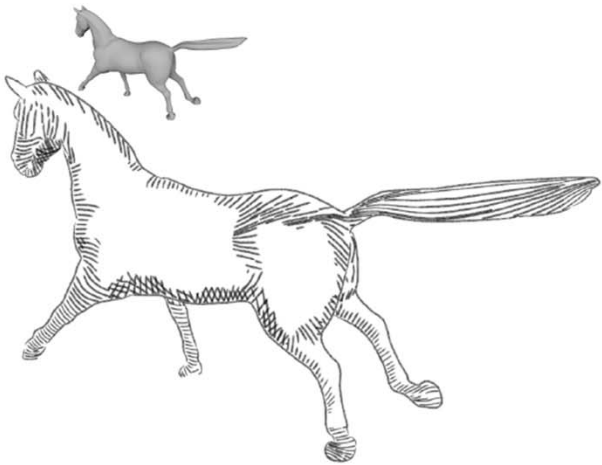
Artist's illustration

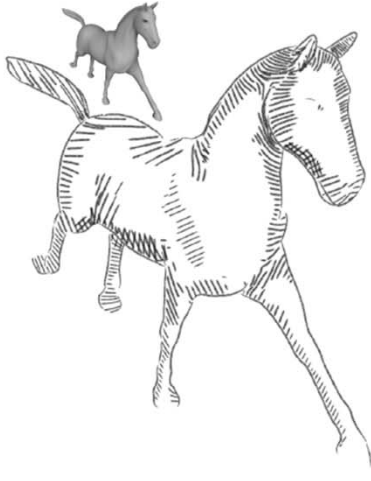
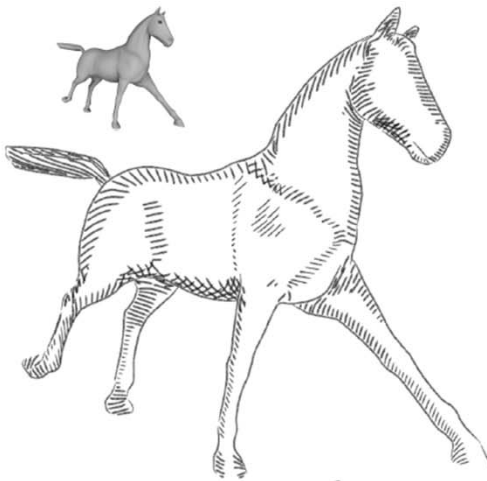
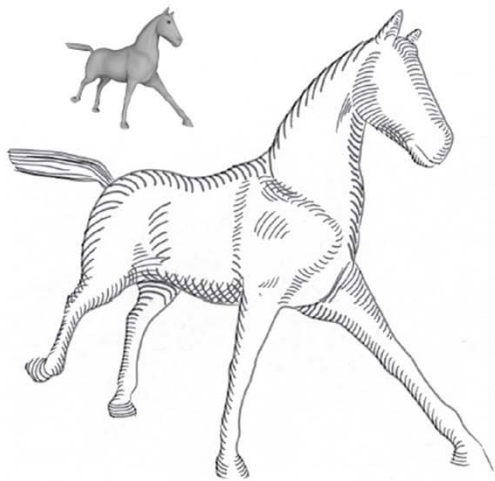


Artist's illustration

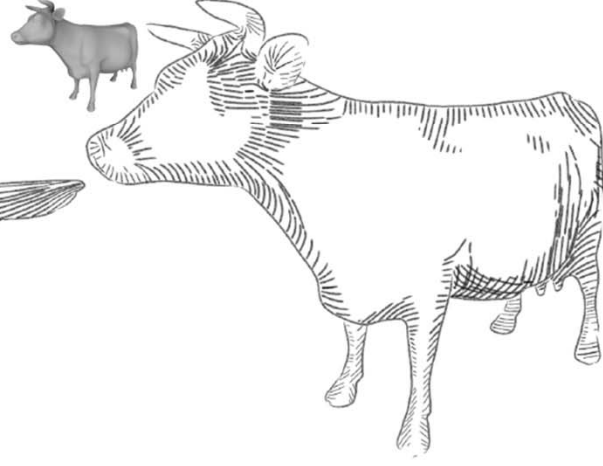
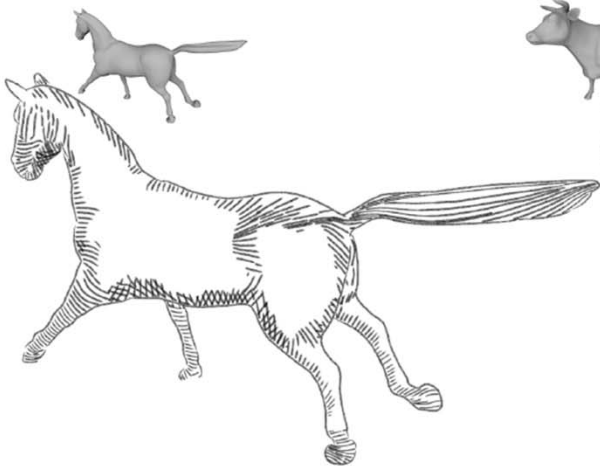


Artist's illustration



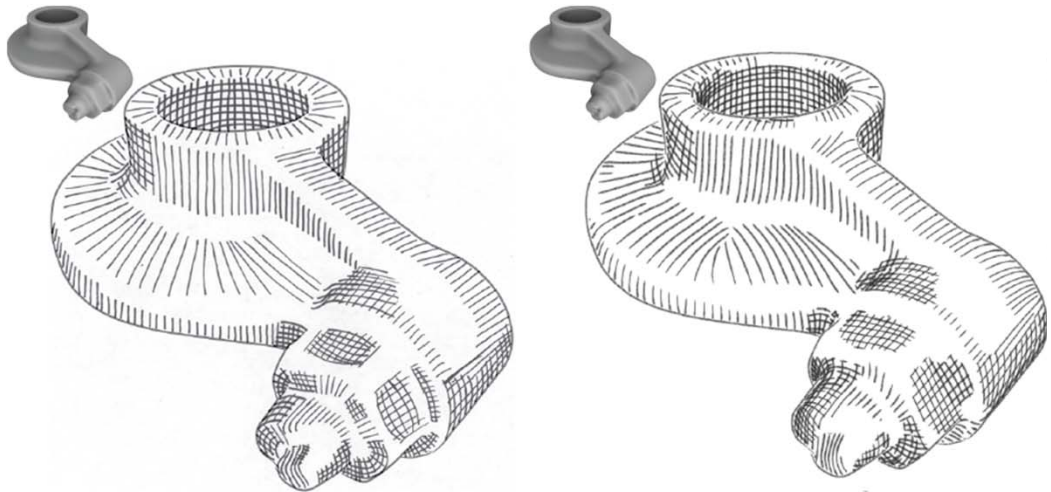


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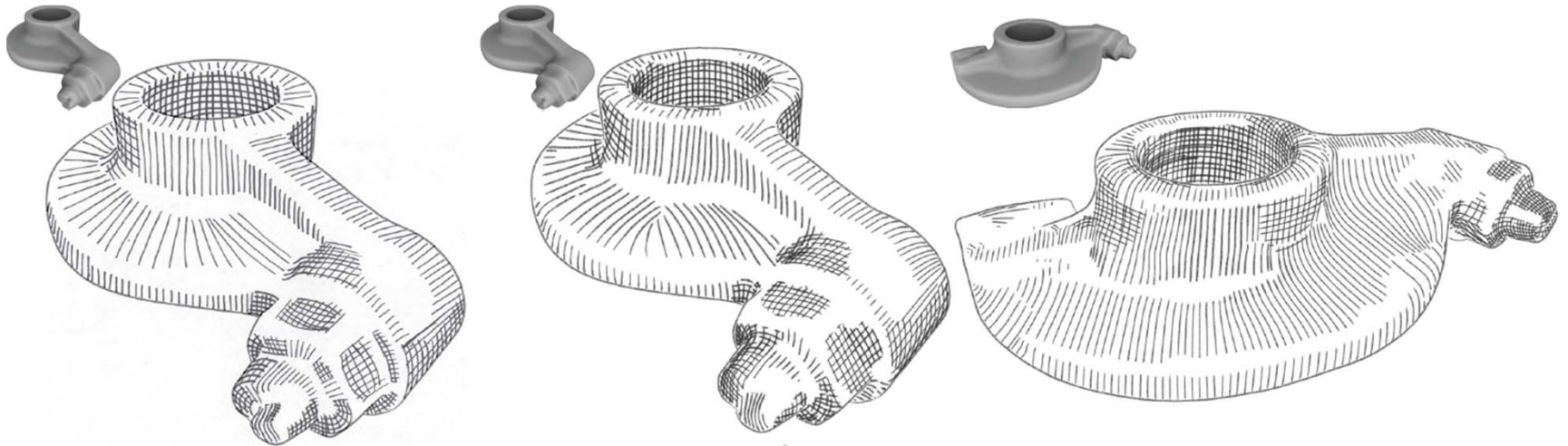




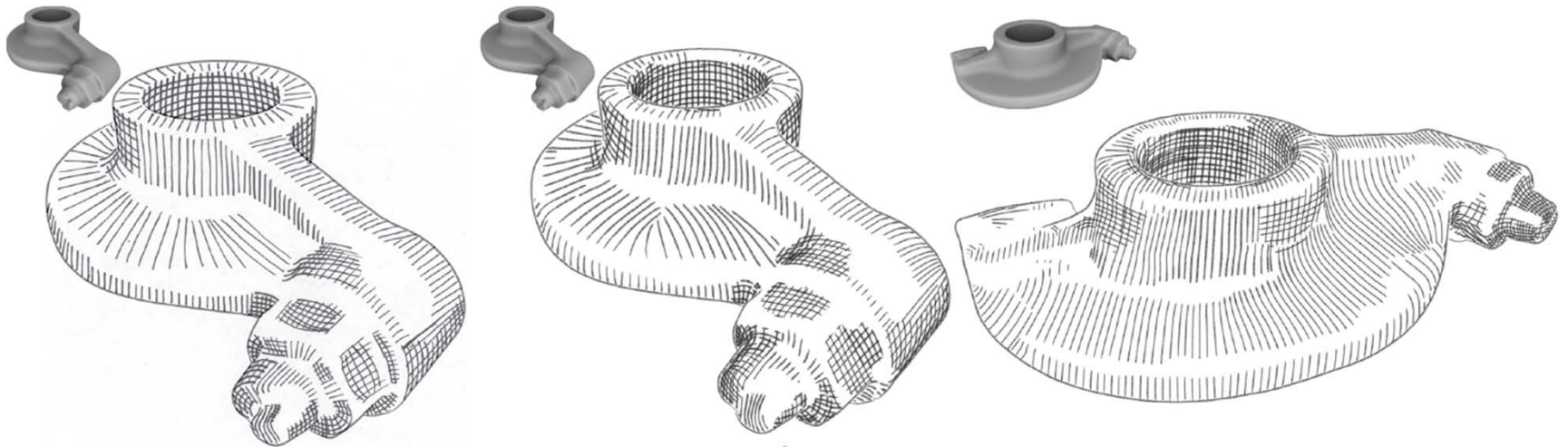
Artist's illustration



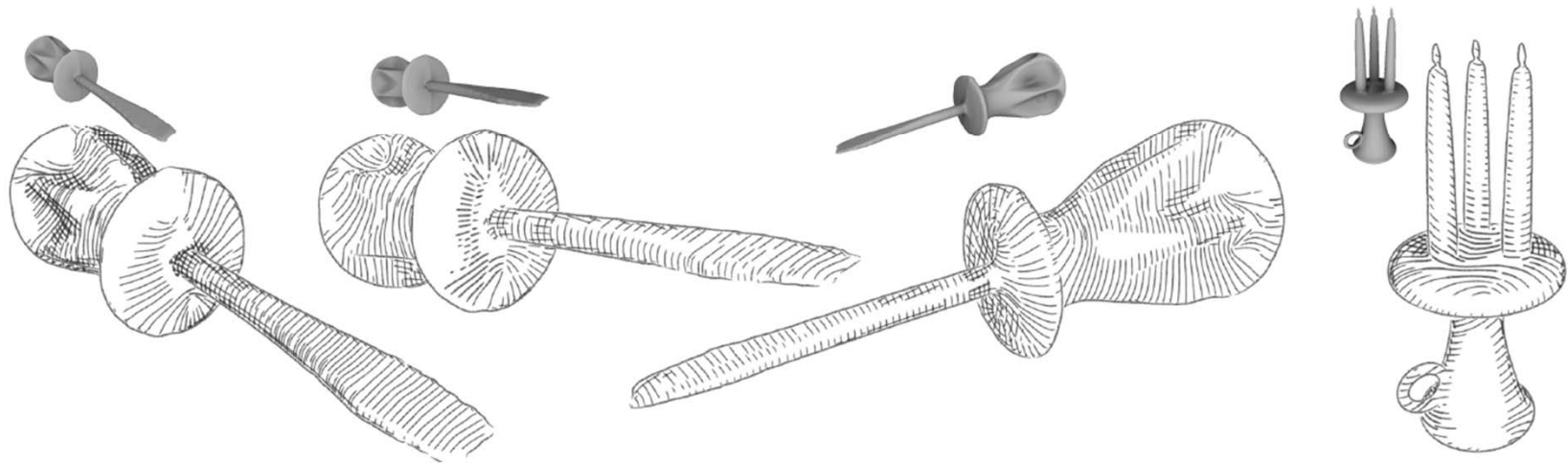
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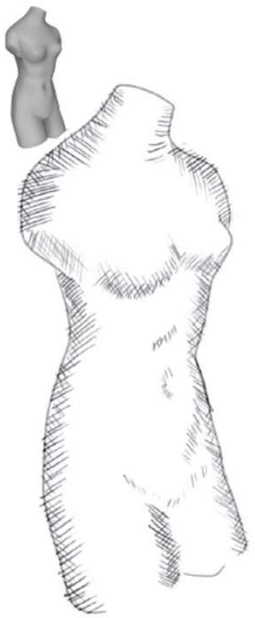


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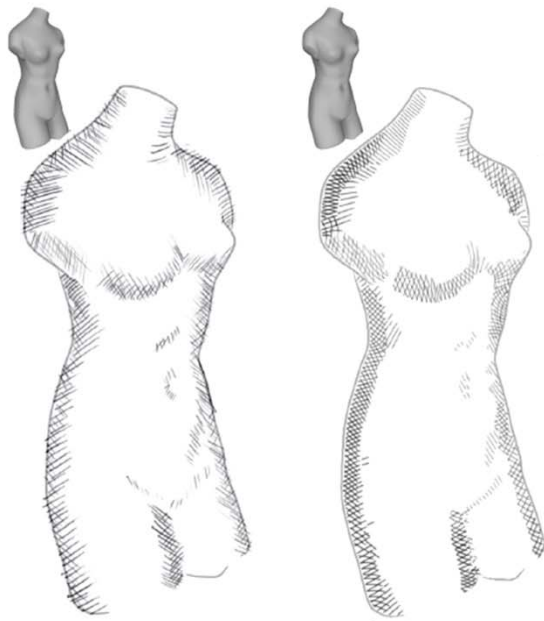


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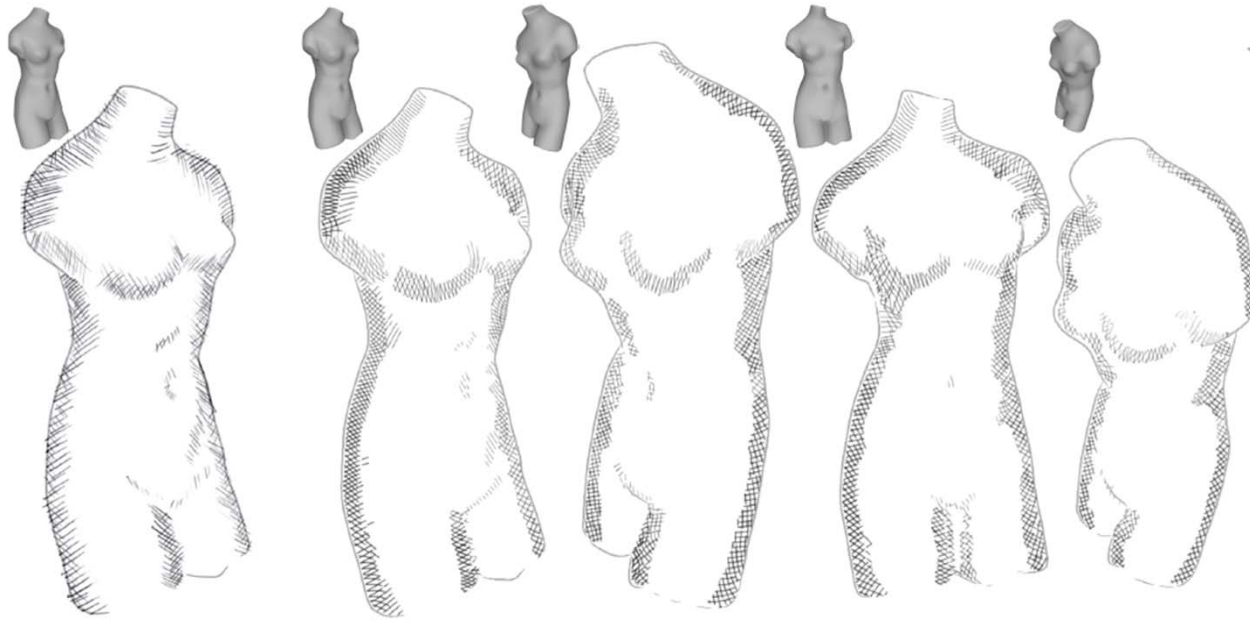




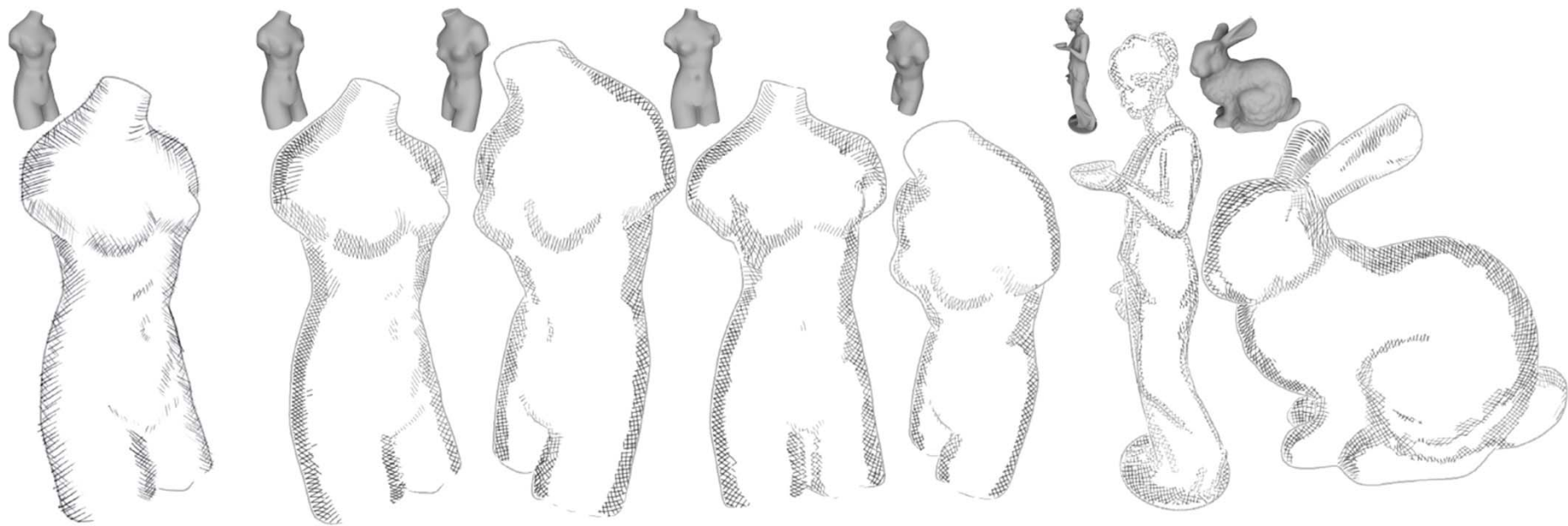
**Artist's
illustration**



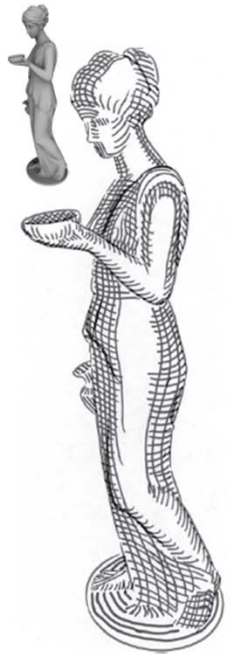
**Artist's
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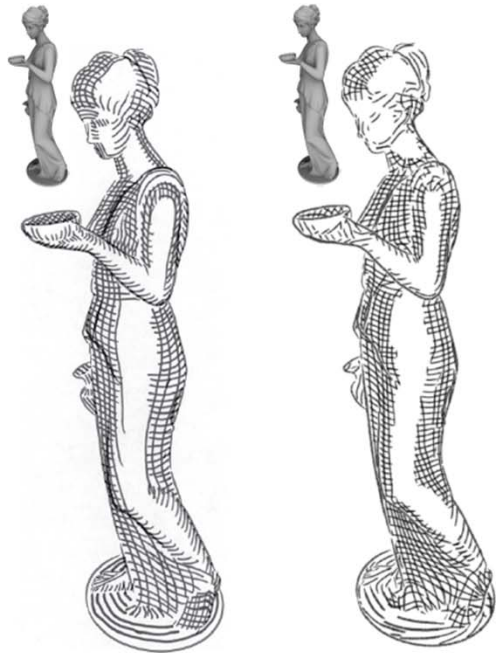
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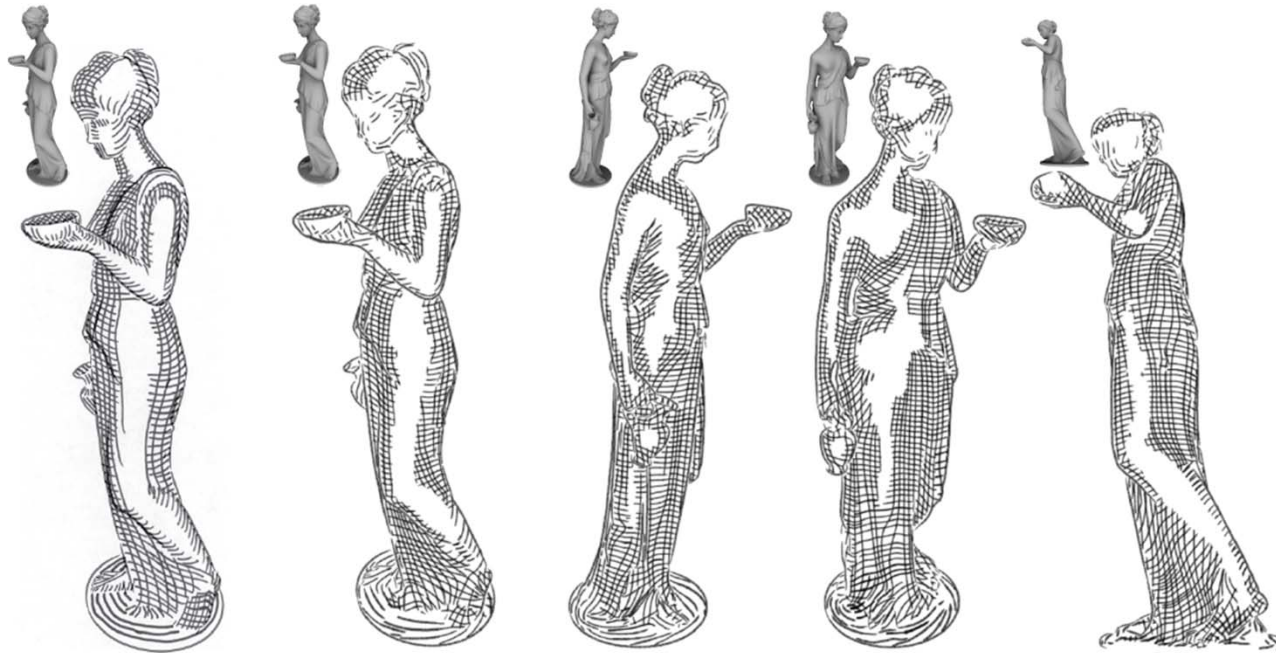
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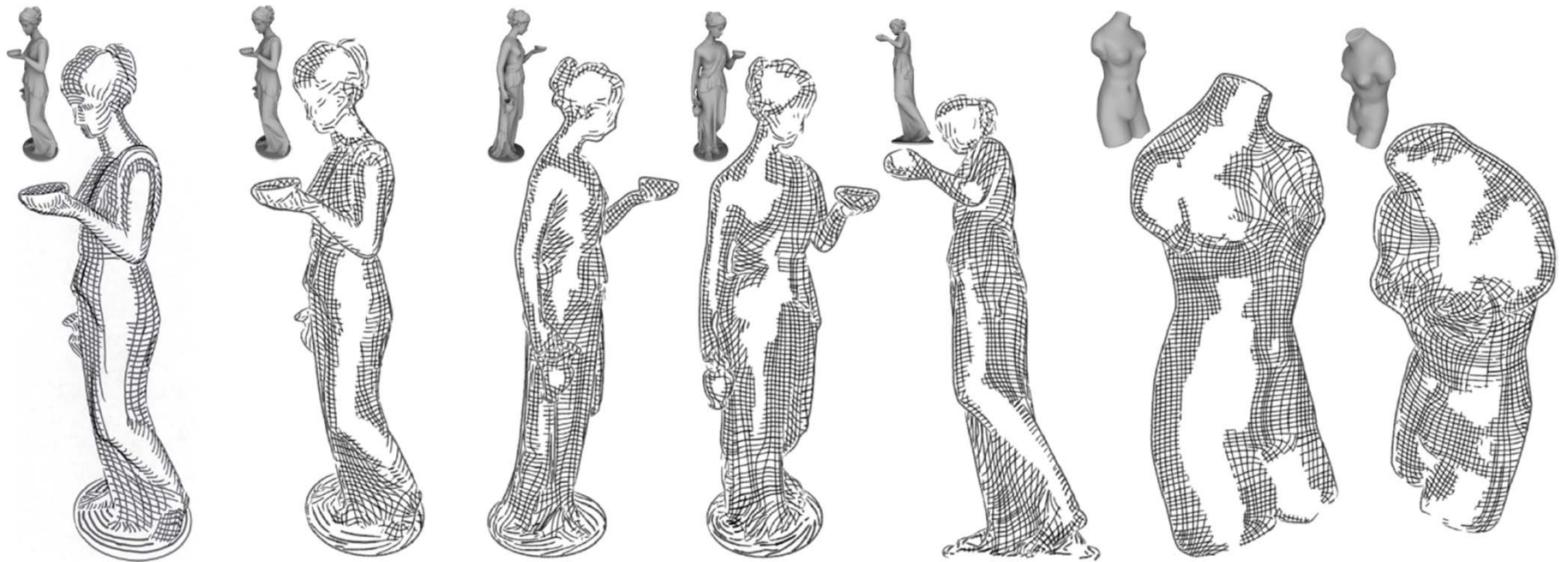
**Artist's
illustration**



**Artist's
illustration**



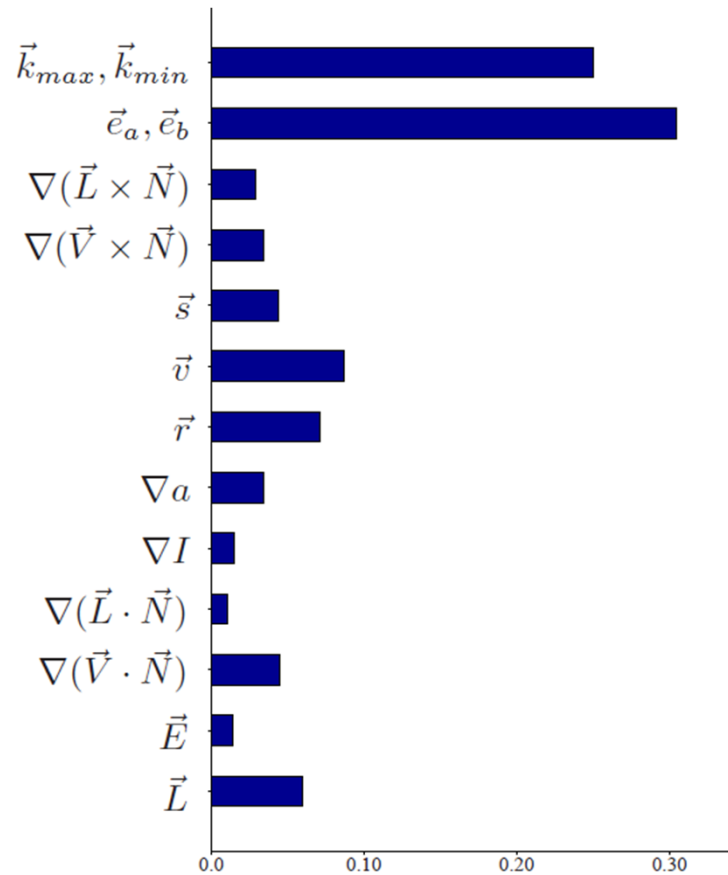
Artist's
illustration



**Artist's
illustration**

Analysis of features used

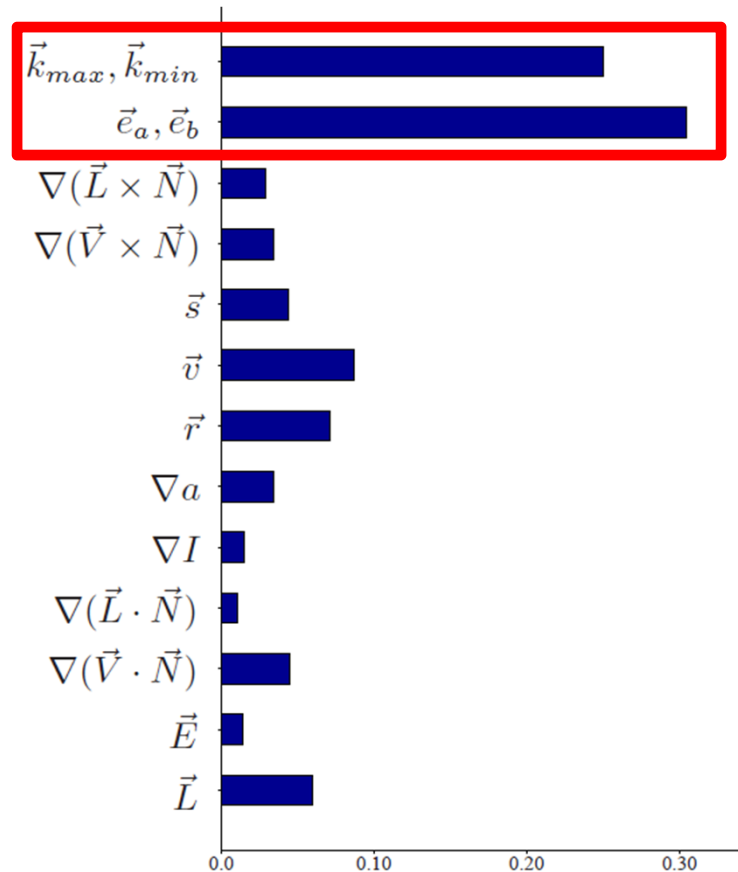
Orientation features:



Analysis of features used

Orientation features:

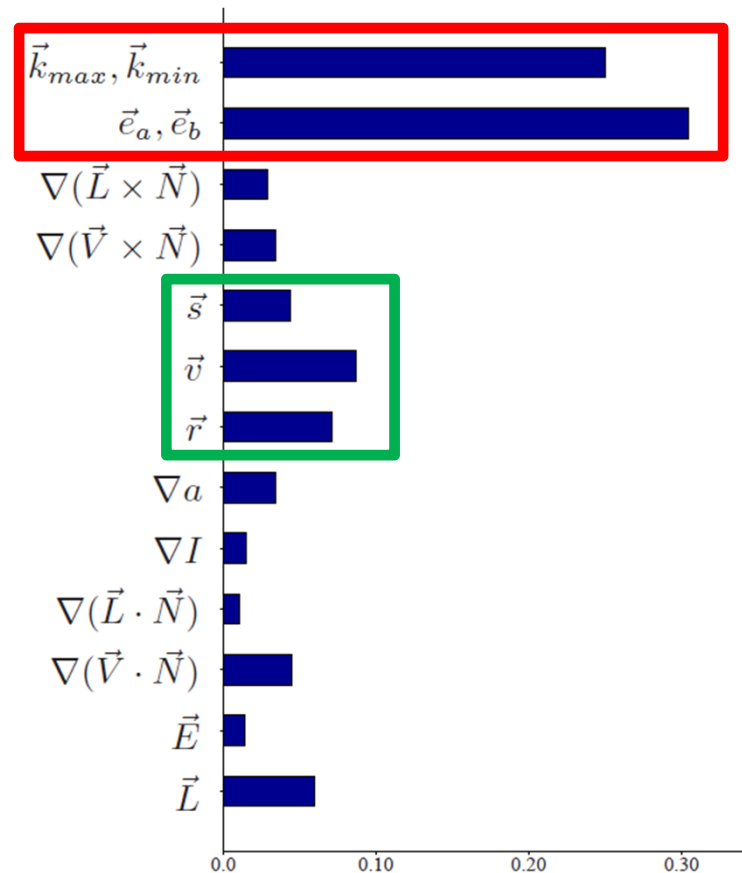
- Principal curvatures and local symmetry axes dominate



Analysis of features used

Orientation features:

- Principal curvatures and local symmetry axes dominate
- Also orientations aligned with feature lines are also important



Analysis of features used

Hatching level: *image intensity, shading features*

Stroke thickness: *shape descriptors, curvature, shading features, image gradients, location of feature lines, depth*

Spacing: *shape descriptors, curvature, derivatives of curvature, shading features*

Intensity: *shape descriptors, image intensity, shading features, depth, location of feature lines*

Length: *shape descriptors, curvature, radial curvature, shading feature, image intensity, image gradient*

Segment label: *shape descriptors*

Summary

- An algorithm that **learns hatching styles**

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- Learns from a **single drawing**

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- An algorithm that **learns hatching styles**
- Learns from a **single drawing**
- Synthesizes hatching illustrations in the input artist's style **for novel views and shapes**

Limitations

- We do not always exactly match the artist's illustration - aspects of hatching style **are lost**

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- Pre-processing stage relies on **thresholds** to robustly extract hatching properties.
- Computation time **is large**
(5h-10h for training, 0.5-1h for synthesis)

Future Work

- Analyze **larger set of drawings**

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- Applications to **field design on surfaces**

Thank you!

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